

# Integrative multi-environmental genomic prediction in apple

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46 **ABSTRACT**

47 Genomic prediction for multiple environments can aid the selection of genotypes suited to  
48 specific soil and climate conditions. Methodological advances allow effective integration of  
49 phenotypic, genomic (additive, non-additive), and large-scale environmental (enviromic) data  
50 into multi-environmental genomic prediction models. These models can also account for  
51 genotype-by-environment interaction, utilize alternative relationship matrices (kernels), or  
52 substitute statistical approaches with deep learning. However, the application of multi-  
53 environmental genomic prediction in apple remained limited, likely due to the challenge of  
54 building multi-environmental datasets and structurally complex models. Here, we applied  
55 efficient statistical and deep learning models for multi-environmental genomic prediction of  
56 eleven apple traits with contrasting genetic architectures by integrating genomic- and  
57 enviromic-based model components. Incorporating genotype-by-environment interaction  
58 effects into statistical models improved predictive ability by up to 0.08 for nine traits  
59 compared to the benchmark model. This outcome, based on Gaussian and Deep kernels,  
60 shows these alternatives can effectively substitute the standard G-BLUP. Including non-  
61 additive and enviromic-based effects resulted in a predictive ability very similar to the  
62 benchmark model. The deep learning approach achieved the highest predictive ability for  
63 three traits with oligogenic genetic architectures, outperforming the benchmark by up to 0.10.  
64 Our results demonstrate that the tested statistical models capture genotype-by-environment  
65 interactions particularly well, and the deep learning models efficiently integrate data from  
66 diverse sources. This study will foster the adoption of multi-environmental genomic  
67 prediction to select apple cultivars adapted to diverse environmental conditions, providing an  
68 opportunity to address climate change impacts.

ORIGINAL UNEDITED MANUSCRIPT

## 69 INTRODUCTION

70 Since the introduction of genomic selection (Meuwissen et al., 2001), the genome-wide  
71 selection based on thousands of markers has resulted in increased genetic gain, and this  
72 approach is progressively becoming an integral component of modern crop breeding programs  
73 (García-Ruiz et al., 2016; Voss-Fels et al., 2019). To predict the genomic estimated breeding  
74 values for genomic selection, marker effects are frequently estimated using the well-  
75 established genomic best linear unbiased predictor (G-BLUP) approach (VanRaden, 2008).  
76 For genomic prediction across environments, increased predictive ability has been  
77 demonstrated by utilizing G-BLUP to incorporate the main marker effects and interaction  
78 effects of markers and environments (Jarquín et al., 2014; Lopez-Cruz et al., 2015). The  
79 interaction between markers and environments provides a mathematical representation of the  
80 natural phenomenon of genotype-by-environment interaction, which results from the  
81 variability in the genotype performance ranking across different environmental conditions.  
82 Despite numerous reports of successful phenotypic performance prediction using molecular  
83 markers in perennial crops such as apple (Kostick et al., 2023; Kumar et al., 2012;  
84 Migicovsky et al., 2016; Muranty et al., 2015), genotype-by-environment interaction has been  
85 often overlooked in genomic prediction of apple traits.

86 The most comprehensive study conducted thus far to investigate the influence of genotype-  
87 by-environment interaction on genomic predictive ability in apple, conducted by Jung et al.  
88 (2022), was achieved by the establishment of the apple reference population, known as the  
89 apple REFPOP (Jung et al., 2020). Across the numerous phenotypic traits assessed in the  
90 apple REFPOP, genotype-by-environment interaction explained up to 24% of the phenotypic  
91 variance, and the incorporation of genotype-by-environment interaction into G-BLUP resulted  
92 in a predictive ability increase of up to 0.07 (Jung et al., 2022). The challenge of building  
93 multi-environmental datasets, coupled with the computational costs tied to the structural  
94 complexity of genomic prediction models accommodating genotype-by-environment  
95 interaction, has likely limited the use of such models in practice.

96 Recent software advances that reduce computational time could enable broader adoption of  
97 multi-environmental genomic prediction models in plant breeding (Costa-Neto, Fritsche-Neto,  
98 et al., 2021; Granato et al., 2018). Empirical comparisons between the well-established R  
99 package ‘BGLR’ (Pérez & de los Campos, 2014) and the newer R package ‘BGGE’ (Granato  
100 et al., 2018), both of which apply the same model structures based on G-BLUP, revealed  
101 comparable predictive abilities, but ‘BGGE’ was up to five times faster (Granato et al., 2018).  
102 In addition to G-BLUP, covariance matrices, alternatively referred to as relationship matrices  
103 or kernels, can be estimated using approaches that capture nonlinearity in the relationships  
104 between phenotype and genotype. The nonlinear Gaussian kernel and the Deep kernel (also  
105 known as the arc-cosine kernel) have demonstrated superior performance compared to G-  
106 BLUP, showing reduced computational time and increased predictive ability in maize and  
107 wheat datasets (Costa-Neto, Fritsche-Neto, et al., 2021; Cuevas et al., 2019).

108 In addition to the commonly used genomic effects of molecular markers, the advancements in  
109 software have introduced straightforward options for incorporating additional sources of  
110 variation into genomic prediction models (Costa-Neto, Fritsche-Neto, et al., 2021; Costa-

111 Neto, Galli, et al., 2021). Using the natural and orthogonal interactions (NOIA) approach,  
112 marker values can be split into additive values and dominance deviations that allow for  
113 orthogonal partition of variances, which implies that the proportions of additive genomic  
114 effects remain constant even when dominance effects are incorporated into the genomic  
115 prediction model (Álvarez-Castro & Carlborg, 2007). The incorporation of dominance effects  
116 into genomic prediction models is typically done by the use of relationship matrices, as  
117 proposed by Vitezica et al. (2013, 2017). Unlike other approaches to construct relationship  
118 matrices for dominance (e.g., Vitezica et al., 2013), the NOIA approach does not assume  
119 Hardy-Weinberg equilibrium, which makes it particularly suitable for populations such as  
120 those resulting from crosses (Vitezica et al., 2017). In apple, the inclusion of non-orthogonal  
121 dominance effects under the assumption of Hardy-Weinberg equilibrium did not affect  
122 predictive ability (Kumar et al., 2015). However, combining dominance effects applying the  
123 NOIA approach along with a fixed effect of inbreeding has demonstrated improved genomic  
124 predictive ability in maize and sugarcane (Roth et al., 2022; Yadav et al., 2021). Additionally,  
125 incorporating non-genetic effects derived from large-scale assessment of environmental  
126 attributes (i.e., envirotyping, resulting in environmental covariates also called enviromic  
127 markers (Cooper et al., 2014; Resende et al., 2021)) into genomic prediction models can  
128 improve the estimation of similarities between environments and genotype-by-environment  
129 interaction. This enhancement not only leads to increased predictive ability, but also offers a  
130 more comprehensive understanding of the complex interplay between genetic and  
131 environmental factors (Costa-Neto, Fritsche-Neto, et al., 2021; Jarquín et al., 2014). The  
132 enviromic-based effects, as well as the marker-based effects expressed as standard genomic,  
133 orthogonal additive and dominance effects, can all be studied as extensions of G-BLUP using  
134 conventional statistical genomic prediction model frameworks, which simplifies their  
135 integration into the modeling process.

136 Deep learning approaches have emerged as an alternative to conventional statistical genomic  
137 prediction models. The literature review of Montesinos-López et al. (2021) on the application  
138 of deep learning for genomic selection showed no distinct superiority of deep learning  
139 approaches in terms of predictive ability compared to conventional genomic prediction  
140 models, unless very large datasets were used. However, deep learning models allow for  
141 effective integration of data from diverse sources, but they can also become impractical for  
142 datasets containing many variables, leading to computational complexity and overfitting. In  
143 plant breeding, datasets comprising thousands of markers are compiled, and dimensional  
144 reduction may help simplify marker information for deep learning (Kick et al., 2023). In the  
145 study by Jurado-Ruiz et al. (2023), the use of a small subset of associated markers was critical  
146 for accurate predictions of apple shape when deploying neural networks. The potential  
147 application of deep learning for multi-environmental genomic prediction of diverse  
148 quantitative apple traits has yet to be examined.

149 This study aims to conduct a comprehensive comparison between conventional statistical  
150 models that integrate genomic- and enviromic-based effects and a deep learning approach for  
151 multi-environmental genomic prediction of apple traits. The subjects of prediction were  
152 eleven quantitative traits related to phenology, productivity, and fruit quality, which were  
153 measured from the apple REFPOP during five years at up to five locations, i.e., up to 25

154 environments (defined as combinations of location and year). The increased extent of the  
 155 apple REFPOP dataset across environments allows an evaluation of different modeling  
 156 techniques to harness the full potential of these data for accurate prediction of phenotypic  
 157 traits. The main objectives of the study were: (i) to evaluate the relative contribution of  
 158 different model components, i.e., random effects and feature streams, for the statistical and  
 159 deep learning genomic prediction models, and (ii) to assess and compare predictive abilities  
 160 of these models. By addressing these two crucial factors, this research aims to provide  
 161 insights into the strengths and limitations of statistical models and deep learning to identify  
 162 the best modelling solutions for the selection of apple cultivars adapted to diverse  
 163 environmental conditions.

164

## 165 RESULTS

### 166 Dataset composition

167 From the eleven phenotypic traits assessed in the apple REFPOP over five years and at a  
 168 maximum of five locations, two environment-trait combinations were excluded due to very  
 169 low values of the environment-specific clonal mean heritability ( $H^2 < 0.1$ ). The excluded  
 170 combinations included phenotypic measurements for floral emergence in Spain in 2020  
 171 ( $H^2 = 0.036$ ) and flowering intensity in France in 2021 ( $H^2 = 0.002$ ). Consequently,  
 172 phenotypic estimates were generated from a minimum of eight environments for titratable  
 173 acidity, soluble solids content, and fruit firmness, while harvest date, total fruit weight,  
 174 number of fruits, and single fruit weight were evaluated across the maximum number of  
 175 environments, totaling 25 (Table S1). Various shapes of distributions and consistent patterns  
 176 of Pearson's correlations were observed for the adjusted means of phenotypic traits over years  
 177 and locations (Figure 1A, Figure S1, Figure S2).

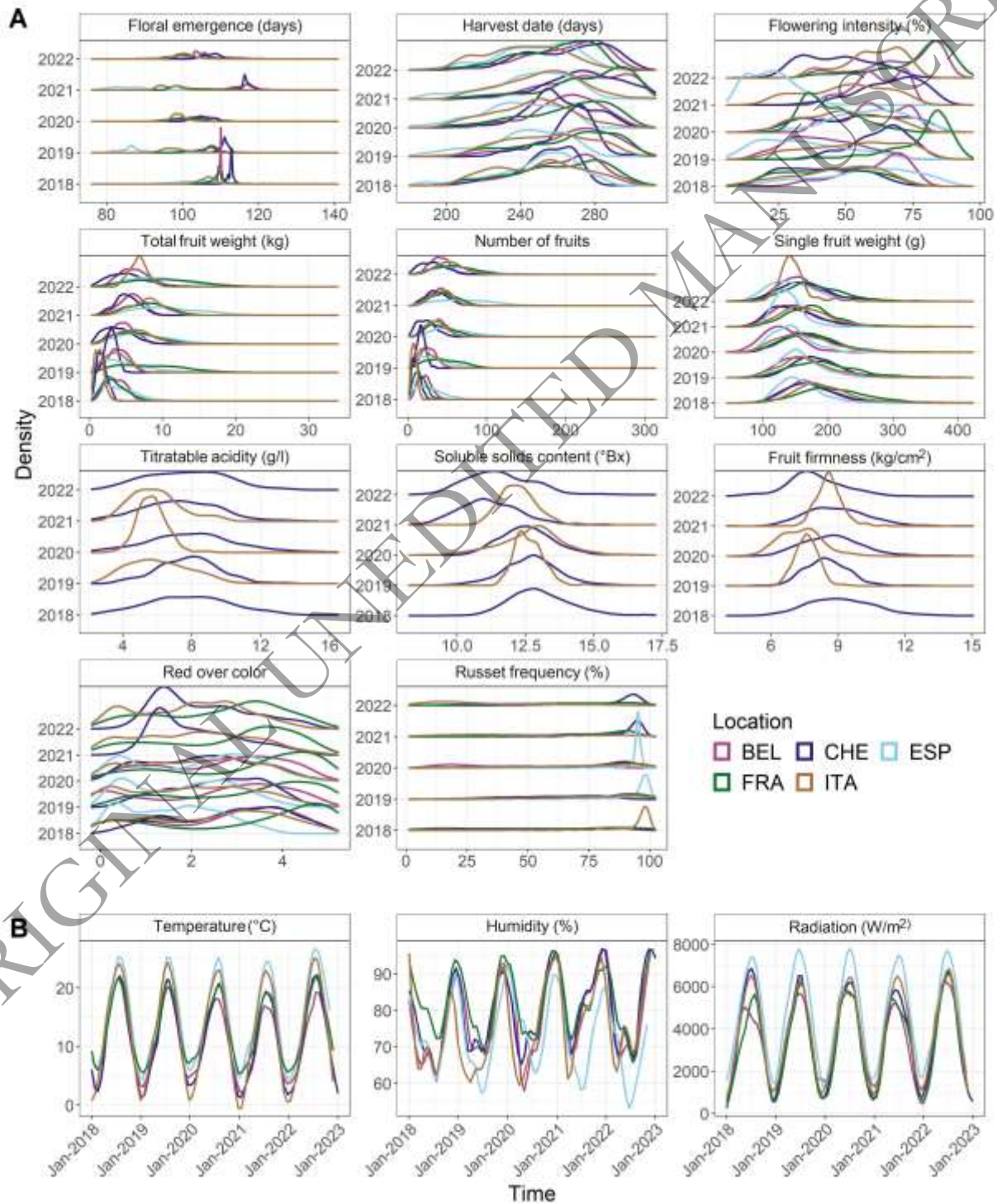
178 For the weather variables, moderate differences were observed in daily temperature means,  
 179 daily humidity means, and daily radiation sums between years and locations (Figure 1B).  
 180 Consequently, these data were summarized based on phenology, meaning the data was split  
 181 into two periods: the first 80 days until 90% of the genotypes flowered, and the following  
 182 days until 90% of the genotypes were harvested (Figure S3). After preprocessing the soil  
 183 variables, the final enviromic dataset included 28 environmental covariates for weather and  
 184 soil.

### 185 Relationship matrices

186 Implementation of the G-BLUP approach resulted in the standard genomic relationship matrix  
 187  $K_G$  (based on standard allele coding with allele dosage values of 0, 1, and 2), the additive  
 188 genomic relationship matrix  $K_A$ , and the dominance genomic relationship matrix  $K_D$  (Figure  
 189 2A, B and C). The heatmaps of these matrices depicted a strong similarity between  $K_G$  and  
 190  $K_A$  (Figure 2A and B). The lower-left quadrant of matrices  $K_G$  and  $K_A$  comprised the apple  
 191 REFPOP accessions, revealing only subtle differences between these genotypes. The upper-  
 192 right quadrant of matrices  $K_G$  and  $K_A$  visualized the apple REFPOP progenies grouped  
 193 according to their biparental origin. The progeny groups were evident in the matrix  $K_D$ , but  
 194 no further strong relationships between genotypes were visually observed.  $K_A$  and  $K_D$

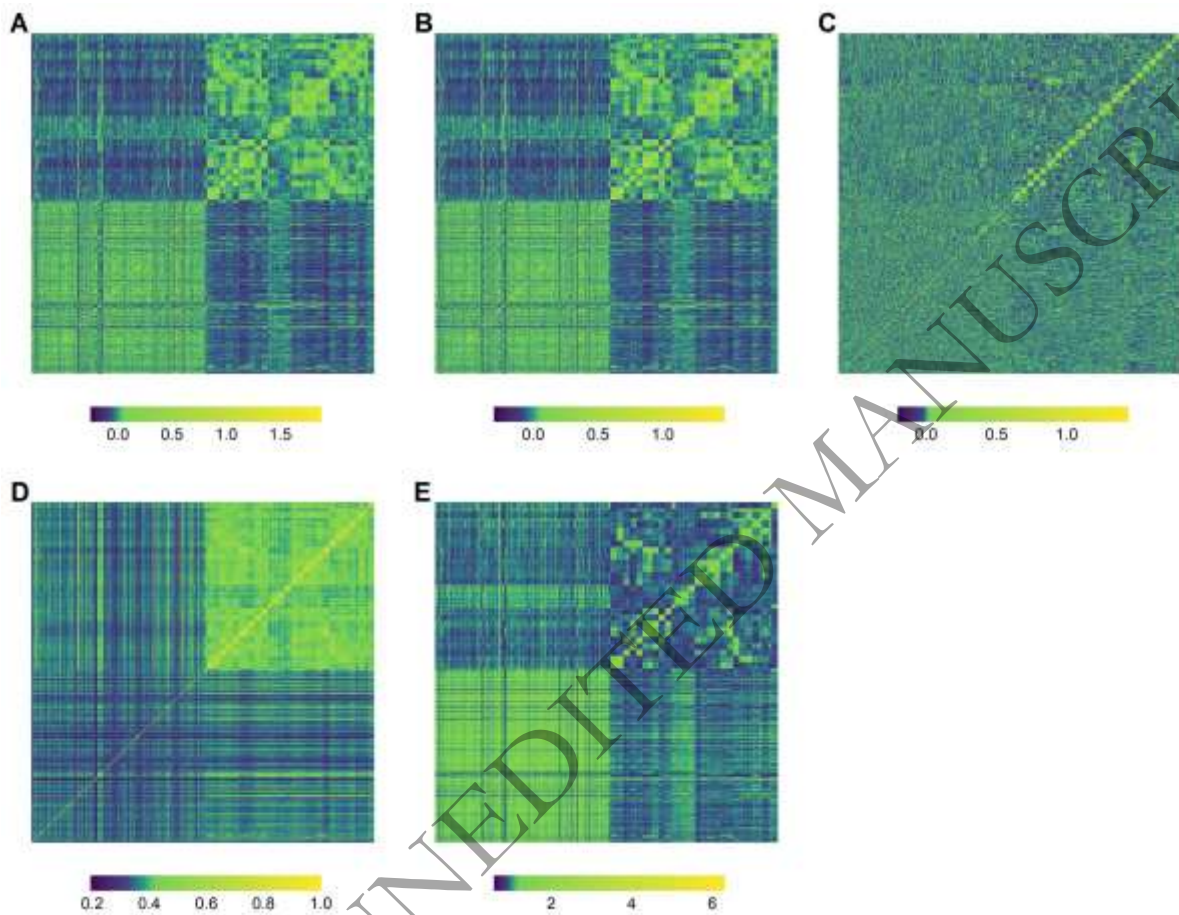


195 showed the mean of their matrix values close to zero and the mean of the diagonal of 1.  
 196 Gaussian kernel and Deep kernel, used as alternative approaches to G-BLUP, resulted in  
 197 matrices  $K_{G_{GK}}$  and  $K_{G_{DK}}$  (Figure 2D and E) that were visually similar to the  $K_G$  and  $K_A$   
 198 matrices implemented using G-BLUP (Figure 2A and B), although some differences were  
 199 observed particularly for the Gaussian kernel approach (Figure 2D). Application of the G-  
 200 BLUP to the enviromic dataset of 28 environmental covariates resulted in the enviromic  
 201 relationship matrix  $K_W$  (Figure 3). Hierarchical clustering of the matrix  $K_W$  showed five  
 202 clusters of environments, each cluster referring to one of the orchard locations.



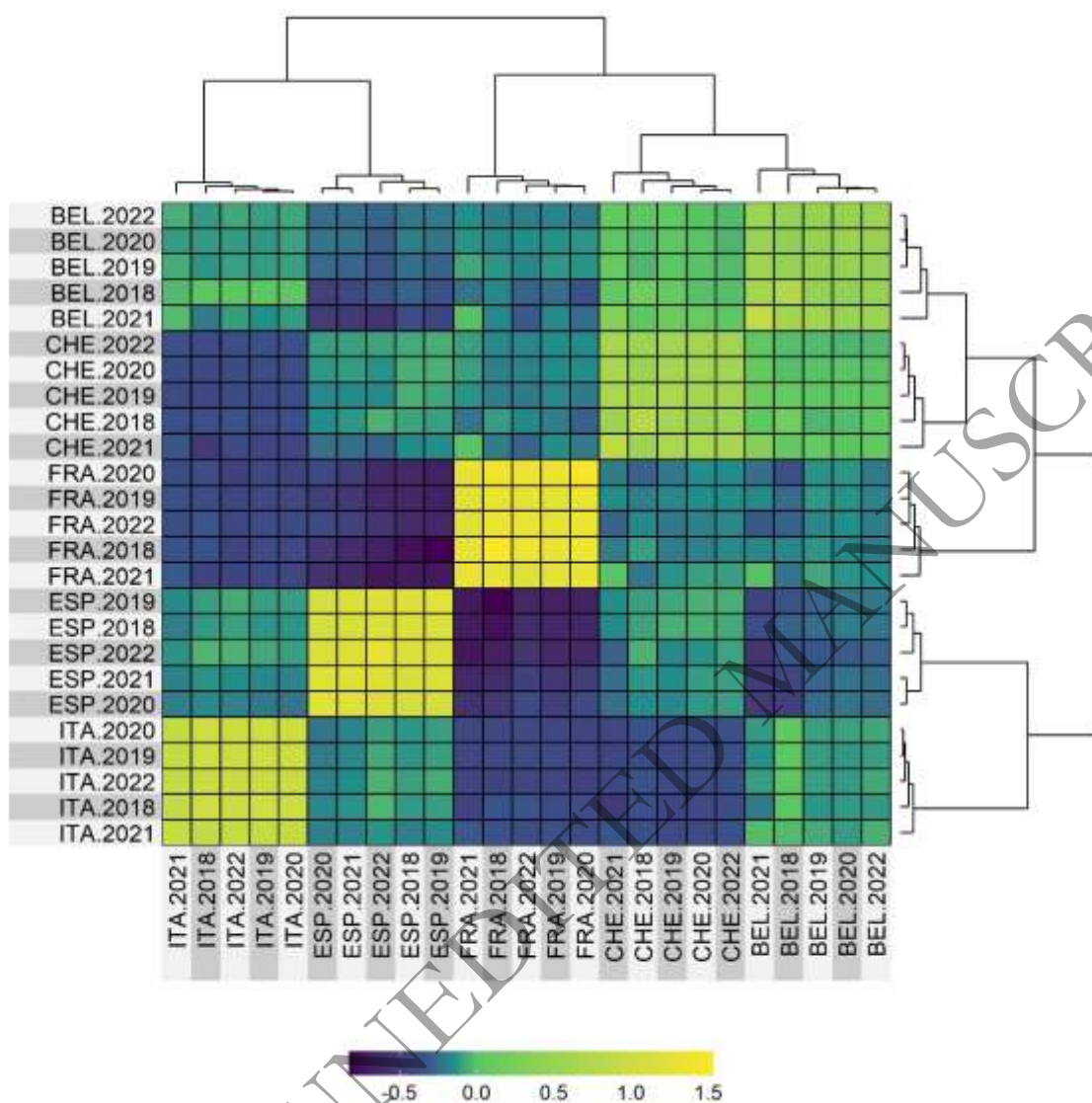
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204 **Figure 1:** Phenotypic and weather data distributions. **A** Density estimates for the adjusted  
 205 means of eleven phenotypic traits from five locations and five years of measurement. The  
 206 locations correspond to Belgium (BEL), Switzerland (CHE), Spain (ESP), France (FRA) and  
 207 Italy (ITA). **B** Local regression curves spanning five years estimated from daily temperature  
 208 means, daily humidity means and daily radiation sums. Colors correspond to legend in A.



209  
 210 **Figure 2:** Heatmaps of the genomic relationship matrices. **A** Standard genomic relationship  
 211 matrix  $K_G$  based on a marker matrix using the standard coding for bi-allelic SNPs (allele  
 212 dosage values of 0, 1, and 2). **B** Additive genomic relationship matrix  $K_A$  based on marker  
 213 matrix using the additive coefficients. **C** Dominance genomic relationship matrix  $K_D$  based  
 214 on marker matrix using the dominance coefficients. The matrices in A–C were constructed  
 215 using the G-BLUP approach. **D** Standard genomic relationship matrix  $K_{GGK}$  constructed  
 216 deploying the Gaussian kernel (GK). **E** Standard genomic relationship matrix  $K_{GDK}$  based on  
 217 the Deep kernel (DK). The lower-left and upper-right quadrants show the apple REFPOP  
 218 accessions and progenies, respectively.





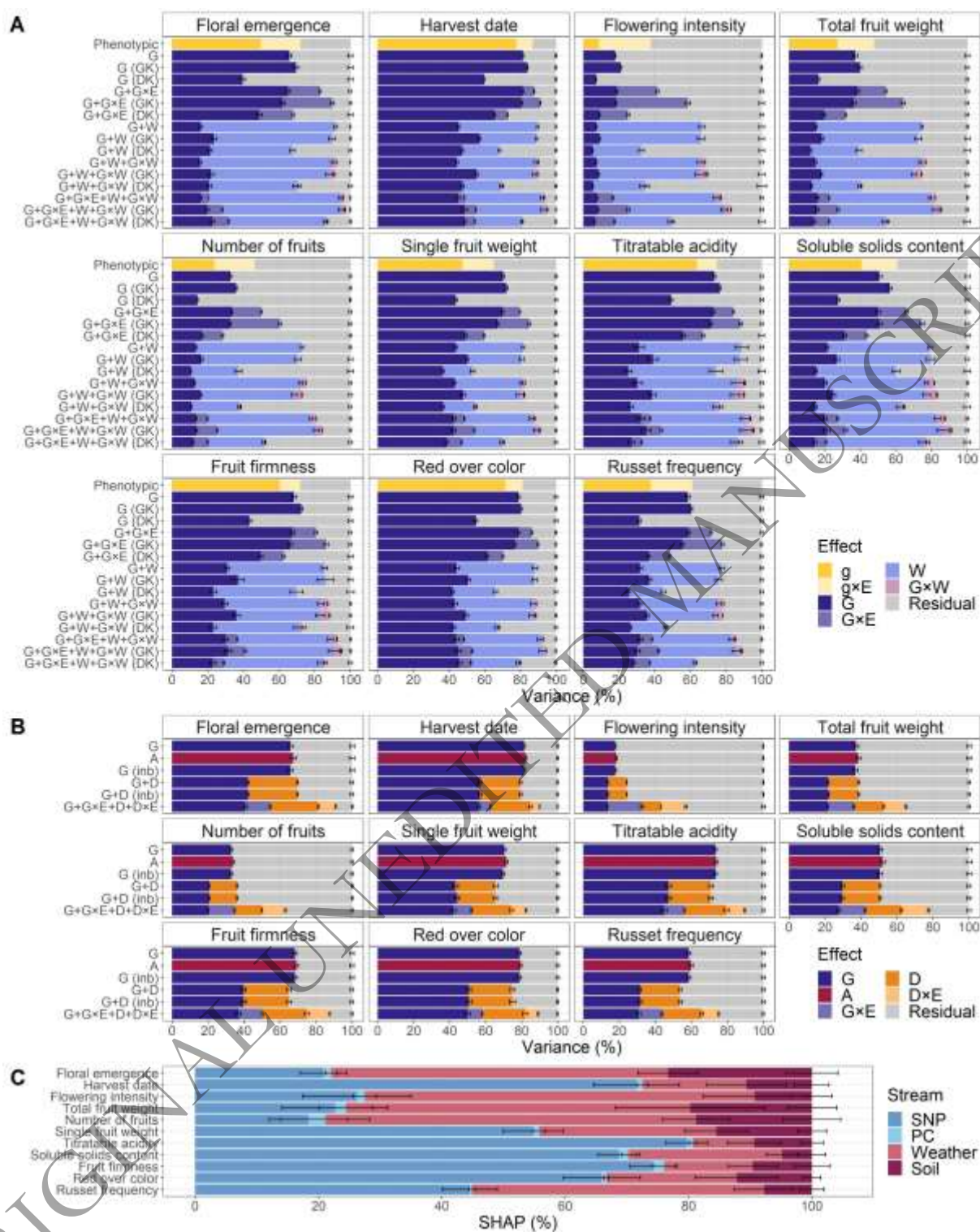
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220 **Figure 3:** The enviromic relationship matrix  $K_W$  constructed from the environmental  
 221 covariates for weather and soil using G-BLUP. Environments (combinations of location and  
 222 year) were grouped applying hierarchical clustering.

### 223 Contribution of the model components

224 Decomposition of the phenotypic variance using linear mixed models by incorporating  
 225 random effects for the vector of genotypes (i.e., genotypic effects) and genotype-by-  
 226 environment interaction, revealed that the proportion of phenotypic variance explained by the  
 227 genotypic effects ranged from 9% for flowering intensity to 78% for harvest date (Figure 4A,  
 228 Table S2). In contrast, the largest proportion of phenotypic variance explained by genotype-  
 229 by-environment interaction was observed for flowering intensity (29%). The lowest  
 230 proportion of genotype-by-environment interaction variance (9%) was found for harvest date.  
 231 The total variance explained by both genotypic and genotype-by-environment interaction  
 232 effects reached 64% on average across traits (Table S3).





233  
234 **Figure 4:** Relative contribution of different model components estimated for eleven traits. **A**  
235 Average proportions of phenotypic variance related to genotypic (g) and genomic (G) effects,  
236 their interactions (×) with the vector of environments (E), the enviromic effects (W), the  
237 interaction effects G×W as well as the residual effect extracted from the statistical genomic  
238 prediction model fits. The relationship matrices for the different effects in the statistical  
239 genomic prediction models were constructed using the G-BLUP approach or, where indicated,  
240 the Gaussian kernel (GK) or Deep kernel (DK). The statistical genomic prediction models  
241 were compared with a model based on phenotypic data (Phenotypic). Error bars correspond to

242 standard deviation around the mean. **B** Average proportions of phenotypic variance related to  
 243 genomic (G), additive (A) and dominance (D) effects, their interactions ( $\times$ ) with the vector of  
 244 environments (E) and the residual effect extracted from the statistical genomic prediction  
 245 model fits. The model structures G and G+D were additionally extended with the fixed effect  
 246 of inbreeding (inb). The relationship matrices for the different effects were based on G-BLUP.  
 247 Error bars correspond to standard deviation around the mean. The results for the benchmark  
 248 model G are the same as shown in A. **C** Relative contribution of the single nucleotide  
 249 polymorphism (SNP), principal component (PC), weather, and soil feature streams estimated  
 250 using Shapley additive explanations (SHAP) for the deep learning genomic prediction model.  
 251 Error bars correspond to standard deviation around the mean.

252 For the statistical genomic prediction based on G-BLUP, linear mixed model structures  
 253 resulted from the application of the relationship matrices  $K_G$ ,  $K_A$ , and  $K_D$ , representing  
 254 genomic (G), additive (A), and dominance (D) effects, respectively. Various proportions of  
 255 phenotypic variance related to these random effects and their interactions ( $\times$ ) were extracted  
 256 from the model fits (Figure 4B, Table S2). Due to its model structure, the simplest genomic  
 257 prediction model (used as a benchmark) was labeled as G, and its random genomic effects  
 258 accounted for an average of 58% of the variance across traits (Table S3). Across all traits,  
 259 model A explained  $\sim$ 1% more variance compared to model G (Table S3). Including the fixed  
 260 effect of inbreeding in model G, leading to model G (inb), resulted in the same proportion of  
 261 explained variance of 58% as for model G (Table S3). For the models G+D and G+D (inb),  
 262 the average total proportion of variance explained by the model components G and D across  
 263 traits was 1% lower than that of model G (Table S3). The model G+G $\times$ E+D+D $\times$ E, on average  
 264 across traits, explained a proportion of variance 21% greater than that explained by model G  
 265 (Table S3).

266 The model G+G $\times$ E based on G-BLUP, including interactions with the environment,  
 267 explained, on average across traits, a proportion of variance 14% greater than that explained  
 268 by model G (Table S3). Specifically, the effect G accounted for variance ranging from 19%  
 269 for flowering intensity to 81% for harvest date, and G $\times$ E explained variance ranging from 6%  
 270 for harvest date to 23% for flowering intensity (Figure 4A, Table S2).

271 The enviromic effects (W) and the interaction effects G $\times$ W were implemented applying the  
 272 relationship matrix  $K_W$  based on G-BLUP in the model structures G+W, G+W+G $\times$ W, and  
 273 G+G $\times$ E+W+G $\times$ W, and these models explained, on average across traits, 24%, 25%, and 30%  
 274 more variance than model G, respectively (Figure 4A, Table S3). For the most complex model  
 275 G+G $\times$ E+W+G $\times$ W, the proportions of variance explained by the interaction effects G $\times$ E and  
 276 G $\times$ W were modest, ranging from 4% to 9% for G $\times$ E and 2% to 4% for G $\times$ W (Table S2).

277 When comparing models based on G-BLUP with their counterparts implementing Gaussian  
 278 kernel using the relationship matrix  $K_{G_{GK}}$  (model structures labeled with GK), the models G  
 279 (GK), G+G $\times$ E (GK), and G+G $\times$ E+W+G $\times$ W (GK) demonstrated an average increase in  
 280 explained variance of 3%, 7%, and 3% across traits, respectively (Figure 4A, Table S3).  
 281 However, the models G+W (GK) and G+W+G $\times$ W (GK) resulted in an average decrease in  
 282 explained variance of up to 1% (Table S3). On average over traits, the model structures based  
 283 on Deep kernel implementing the relationship matrix  $K_{G_{DK}}$  (model structures labeled with

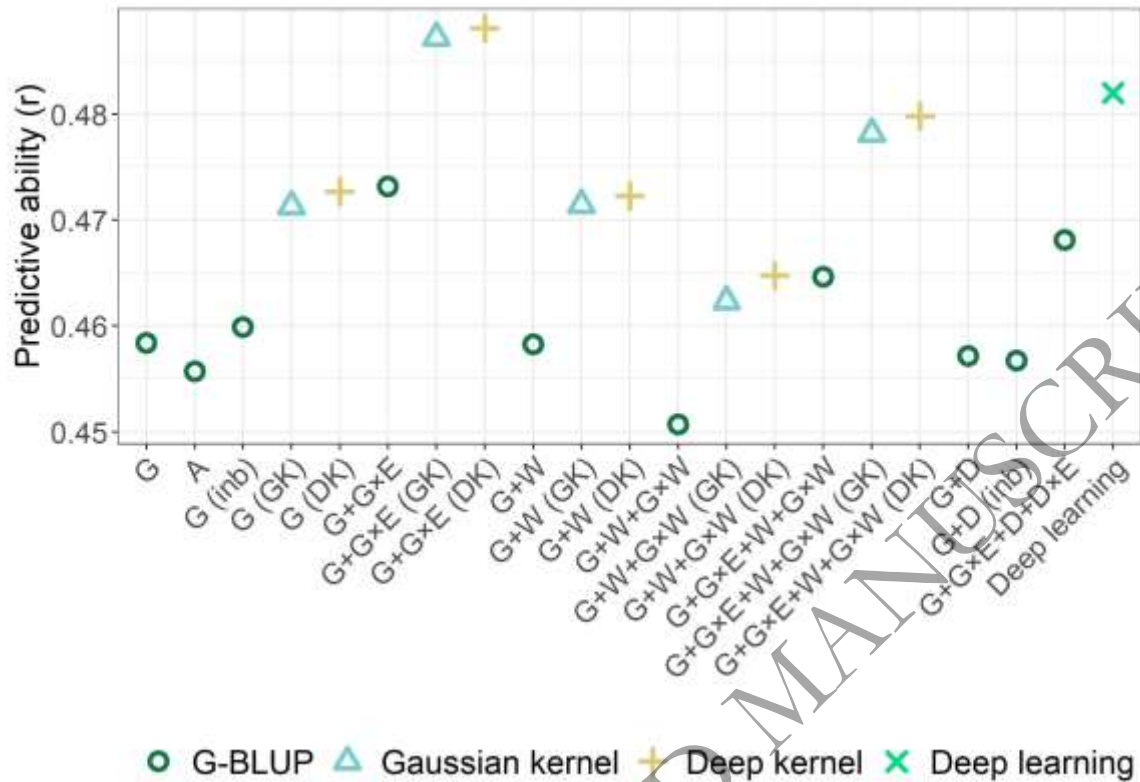
284 DK) exhibited a strong decrease in the proportion of variance explained by the genomic- and  
285 enviromic-based random effects when compared to their counterparts utilizing G-BLUP,  
286 namely -22% for G (DK), -19% for G+G×E (DK), -26% for G+W (DK), -25% for  
287 G+W+G×W (DK), and -17% for G+G×E+W+G×W (Table S3).

288 The applied deep learning genomic prediction model integrated marker and enviromic data  
289 through four feature streams, namely single nucleotide polymorphism (SNP), principal  
290 component (PC), weather, and soil streams, and the estimation of Shapley additive  
291 explanations (SHAP) revealed the relative mean importance of these feature streams (Figure  
292 4C, Table S4). Across all traits, the relative SHAP contributions were 50% for the SNP  
293 stream, 1% for the PC stream, 36% for the weather stream, and 13% for the soil stream. The  
294 relative SHAP contribution for the SNP stream ranged from 18 to 26% for floral emergence  
295 and the productivity traits (flowering intensity, total fruit weight and number of fruits) to 80%  
296 for titratable acidity. For the PC stream, the relative SHAP contribution ranged between 0%  
297 for russet frequency and 3% for number of fruits. The lowest weather stream contribution of  
298 10% was found for titratable acidity, while the largest contribution of the weather stream of 55  
299 to 63% was found for floral emergence and the productivity traits (flowering intensity, total  
300 fruit weight and number of fruits). The relative SHAP contribution for the soil stream ranged  
301 between 5% for soluble solids content and 19 to 23% for floral emergence and two  
302 productivity traits (total fruit weight and number of fruits). An abundance of SNPs displaying  
303 high absolute mean SHAP were found for harvest date, titratable acidity and red over color  
304 (Figure S4, Figure S5). For harvest date, three SNPs with the highest absolute mean SHAP of  
305 0.002 were located on chromosome 3 at 29.2 Mb (AX-115250472), 30.7 Mb (AX-  
306 115366114), and 30.8 Mb (AX-115233388). The three SNPs with the highest absolute mean  
307 SHAP of 0.003 for titratable acidity were found on chromosome 8 at 10.7 Mb (AX-  
308 115276534), 10.8 Mb (AX-115254093), and 11.8 Mb (AX-115519462). For red over color,  
309 the three SNPs with the highest absolute mean SHAP of 0.005 were located on chromosome 9  
310 at 33.8 Mb (AX-105213720, AX-115558498), and 35.6 Mb (AX-115370846).

### 311 **Predictive ability**

312 Assessment of genomic prediction model performance using five-fold cross-validation  
313 showed that the average predictive ability across traits ranged from 0.45 to 0.49 for the  
314 compared models (Figure 5, Table S5). Based on these average predictive abilities, the model  
315 G+W+G×W emerged as the least efficient, with an average predictive ability across traits of  
316 0.45. Models A, G (inb), G+W, G+W+G×W (GK), G+W+G×W (DK), G+G×E+W+G×W,  
317 G+D, and G+D (inb) demonstrated equivalent average predictive ability across traits, with a  
318 value of 0.46, comparable to the benchmark model G based on G-BLUP. Average predictive  
319 ability across traits of 0.47 was found for the models G (GK), G (DK), G+G×E, G+W (GK),  
320 G+W (DK), and G+G×E+D+D×E. The models G+G×E+W+G×W (GK), G+G×E+W+G×W  
321 (DK) and deep learning provided additional improvement with the average predictive ability  
322 across traits of 0.48. The models G+G×E (GK) and G+G×E (DK) showed the highest average  
323 predictive ability across traits of 0.49.

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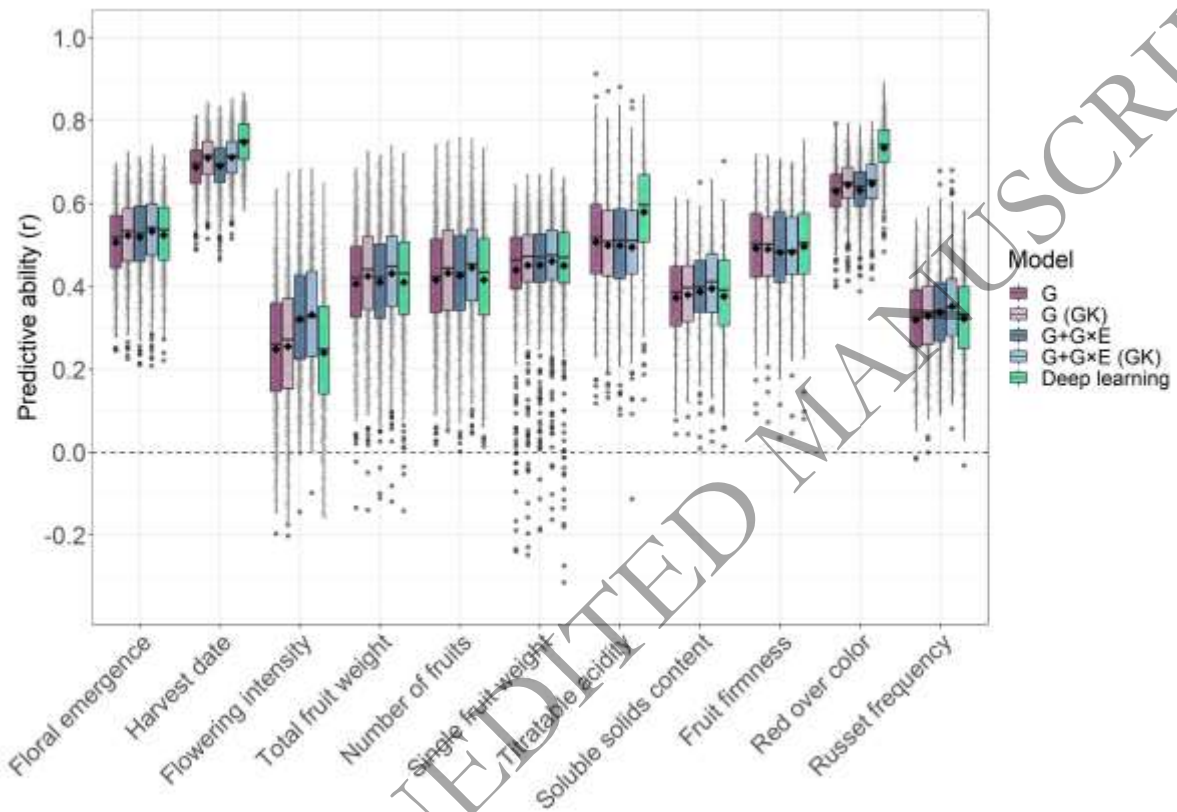
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326 **Figure 5:** Comparison of predictive ability averaged across all studied traits. The statistical  
 327 genomic prediction models were based on combinations of the genomic (G), additive (A),  
 328 dominance (D), and enviromic (W) effects, interactions (×) with the vector of environments  
 329 (E), and interactions between the genomic and enviromic effects (G×W). The model  
 330 structures G and G+D were additionally extended with the fixed effect of inbreeding (inb).  
 331 The relationship matrices for the different effects in the statistical genomic prediction models  
 332 were constructed using the G-BLUP approach or, where indicated, the Gaussian kernel (GK)  
 333 or Deep kernel (DK). The y-axis was truncated to provide a detailed model comparison. See  
 334 Table S6 for a comparison of the predictive ability for each trait.

335 For four models selected for an in-depth comparison with the benchmark model G based on  
 336 their performance and characteristics (G (GK), G+G×E, G+G×E (GK), and deep learning),  
 337 strong differences in average predictive ability were observed among the examined traits  
 338 (Figure 6, Table S6). Flowering intensity and russet frequency were at the lower end of the  
 339 predictive ability spectrum, while harvest date and red over color were at the upper end.  
 340 Compared to model G, the model G (GK) showed an increase in average predictive ability of  
 341 0.01 to 0.02 for most traits, but no improvement in predictive ability was found using this  
 342 model for titratable acidity and fruit firmness. Model G+G×E led to an increase in average  
 343 predictive ability of 0.07 for flowering intensity and 0.01 to 0.02 for floral emergence,  
 344 number of fruits, single fruit weight, soluble solids content, and russet frequency. It showed  
 345 no improvement for harvest date, total fruit weight, titratable acidity, fruit firmness, and red  
 346 over color. Model G+G×E (GK) demonstrated an additional improvement in average  
 347 predictive ability of 0.01 to 0.02 compared to model G+G×E for all traits, except for titratable  
 348 acidity and fruit firmness. For these two traits, the incorporation of the G×E effect led to a  
 349 decrease in average predictive ability by 0.01 in both tested models, G+G×E and G+G×E



350 (GK), compared to model G. The deep learning genomic prediction model demonstrated  
 351 higher predictive abilities than model G for five out of the eleven traits studied. For harvest  
 352 date, titratable acidity and red over color, the deep learning genomic prediction model  
 353 outperformed all statistical genomic prediction models tested. The increase in average  
 354 predictive ability compared to model G was 0.06 for harvest date, 0.07 for titratable acidity,  
 355 and 0.10 for red over color.



356  
 357 **Figure 6:** Boxplots of predictive abilities for eleven traits estimated using statistical and deep  
 358 learning genomic prediction models. The statistical genomic prediction models were based on  
 359 combinations of the genomic effects (G) and their interactions with the vector of  
 360 environments (G×E). The relationship matrices for the different effects in the statistical  
 361 genomic prediction models were constructed using the G-BLUP approach or, where indicated,  
 362 the Gaussian kernel (GK). Twenty-five predictive ability estimates were generated for each  
 363 available environment (up to 625 estimates per trait), and their average was displayed as black  
 364 diamonds for each model and trait. Jittered points (grey) show all predictive ability estimates  
 365 for each trait.

366

## 367 DISCUSSION

368 This study provides insights into the complexities of multi-environmental genomic prediction  
369 in quantitative apple traits. The incorporation of different sources of variation in the form of  
370 model components, and the comparison of predictive abilities between statistical genomic  
371 prediction models and a deep learning approach contribute to advancing the understanding of  
372 efficient genomic prediction methodologies. The findings highlight the need for a nuanced  
373 approach, considering the specific traits and modelling approaches in plant breeding  
374 applications.

### 375 **Modelling genotype-by-environment interaction**

376 In the context of genomic prediction across environments (defined as combinations of  
377 location and year), this work underscored a detectable improvement in predictive ability when  
378 employing genomic prediction models based on G-BLUP that integrate both main marker  
379 effects and the interaction effects of markers and environments, as it has been described by  
380 previous studies (Jarquín et al., 2014; Jung et al., 2022; Lopez-Cruz et al., 2015). Compared  
381 to the benchmark genomic prediction model implementing exclusively the main marker  
382 effects, Jung et al. (2022) reported up to 0.07 increase in predictive ability for apple traits by  
383 integrating the random effects for G×E using the software package ‘BGLR’ (Pérez & de los  
384 Campos, 2014). In this study deploying the newer software ‘BGGE’ (Granato et al., 2018), an  
385 analogous model comparison based on the same plant material but including two additional  
386 years of phenotypic data showed comparable improvements in predictive ability of up to 0.07.  
387 Average predictive ability across eleven studied traits for models incorporating G×E using G-  
388 BLUP was 0.01 lower compared to the average predictive ability for the same traits reported  
389 previously (Table S6, Jung et al., 2022). As the predictive ability of G×E models based on G-  
390 BLUP was similar in ‘BGLR’ and ‘BGGE’ (Granato et al., 2018), the difference in predictive  
391 ability was likely due to the changes in the phenotypic dataset between the compared studies.

392 The inclusion of G×E effects led to an increase in predictive ability, which was associated  
393 with a higher proportion of variance explained by the random effects (Figure 4). However, the  
394 improvement in predictive ability was disproportionately smaller compared to the increase in  
395 explained variance. This discrepancy between the substantial rise in explained variance and  
396 the modest gain in predictive ability was observed across all the statistical genomic prediction  
397 models studied, contrary to expectations (Costa-Neto, Fritsche-Neto, et al., 2021). It might be  
398 explained by the fact that variance was estimated using the training sets, while predictive  
399 ability was evaluated on the validation sets. This suggests that the model, although effectively  
400 capturing patterns in the training set, did not generalize well to the validation set, resulting in  
401 limited improvements in predictive ability for the validation set.

### 402 **Dominance effects**

403 Previous study by Kumar et al. (2015) showed similar predictive ability between genomic  
404 prediction models with and without dominance effects when analyzing quantitative traits in  
405 apple. In their work, dominance effects were modeled using nonorthogonal coefficients and  
406 under the assumption of Hardy-Weinberg equilibrium. In contrast, our study implemented  
407 orthogonal dominance coefficients that do not assume Hardy-Weinberg equilibrium, leading

408 to the expectation of improved predictive ability (Yadav et al., 2021; Roth et al., 2022).  
409 However, despite this implementation, only limited improvement in predictive ability was  
410 observed for the G+D and G+G×E+D+D×E models, as well as for models incorporating  
411 inbreeding (Table S5).

412 Orthogonal partitioning of variances implies that the proportions of additive genomic effects  
413 remain unchanged when additional effects, such as dominance, are introduced into the  
414 genomic prediction model (Álvarez-Castro & Carlborg, 2007). Despite using the NOIA  
415 procedure for orthogonal partitioning of additive and dominant variances that does not assume  
416 Hardy-Weinberg equilibrium (Álvarez-Castro & Carlborg, 2007; Vitezica et al., 2017), our  
417 results indicate nonorthogonality when comparing models G, A and G+D. Specifically, the  
418 comparison of these models showed a 22% reduction in the average proportion of variance of  
419 the genomic effects across all studied traits for model G+D, and a 1% decrease in the total  
420 average variance explained by model G+D (Table S2, Table S3). Similar results have been  
421 found in different crops, where the extension of models analogous to G and A with dominance  
422 effects (orthogonal or nonorthogonal, assuming or not assuming Hardy-Weinberg  
423 equilibrium) has often led to reduced estimates of additive variance components, and  
424 sometimes even to a reduction in the total explained variance, falling below the levels  
425 achieved by the simpler models G and A (Amadeu et al., 2020; Costa-Neto, Fritsche-Neto, et  
426 al., 2021; Kumar et al., 2015; Roth et al., 2022; Yadav et al., 2021). While an earlier study  
427 showed that dominance variance was overestimated when inbreeding was not taken into  
428 account (Vitezica et al., 2018), our variance decomposition showed no signs of upwardly  
429 biased estimates of dominance variance in model G+D compared to G+D (inb) (Table S2).  
430 Our results likely point to potential problems in variance estimation caused by linkage  
431 disequilibrium (Roth et al., 2022; Vitezica et al., 2017), which is prevalent in breeding  
432 material such as that contained in the apple REFPOP. Beside the violation of the assumption  
433 of linkage equilibrium, the incorrect variance partitioning may have resulted from fitting  
434 multiple genetic and genotype-by-environment interaction effects within the framework of  
435 multi-environmental genomic prediction, which deserves further investigation. A preliminary  
436 analysis outside the scope of this study indicated that orthogonality was restored when  
437 conducting analyses on across-location clonal values (results not shown).

438 Compared to other approaches to modelling non-additive effects, the NOIA approach retains  
439 the advantage of allowing deviations from the Hardy-Weinberg equilibrium (Vitezica et al.,  
440 2017). In contrast, the method by VanRaden (2008) for constructing standard genomic  
441 relationship matrices assumes that the population is unselected and in Hardy-Weinberg  
442 equilibrium. However, instead of using allele frequencies from a hypothetical unselected  
443 population in Hardy-Weinberg equilibrium, the standard genomic relationship matrix  $K_G$   
444 was computed using observed allele frequencies from our training population. Although this  
445 assumption is violated for  $K_G$ , our study showed a strong similarity between  $K_G$  and the  
446 additive genomic relationship matrix  $K_A$  that was based on the NOIA approach (Figure 2),  
447 along with the near-identical average predictive abilities across traits observed for models G  
448 and A (Figure 5). These outcomes may suggest that any potential violation of Hardy-Weinberg  
449 equilibrium in the studied population had minimal impact on genomic prediction. In addition,  
450 despite the similarity between  $K_G$  and  $K_A$ , differences in the prediction error variance of the

451 genomic-estimated breeding values could arise when using these matrices in genomic  
452 prediction models (Strandén & Christensen, 2011). However, these differences were not  
453 investigated in this study.

#### 454 **Non-genetic effects from envirotyping**

455 As suggested by moderate differences in daily weather variables among years and locations,  
456 and the low differentiation between environments within a location in the enviromic  
457 relationship matrix, environmental covariates discriminated well between locations but  
458 weakly between specific environments. This could likely be explained by the larger number  
459 of soil covariates (22) than weather covariates (6), and the lack of variability between years  
460 for the soil covariates due to their single measurement at each orchard location in 2016.  
461 Additionally, the precipitation variable, which could have aided in distinguishing between  
462 environments, had to be excluded from the analysis. This decision was prompted by the  
463 confounding of precipitation with irrigation at some apple REFPOP locations. Nevertheless,  
464 the enviromic-based effects explained a substantial part of the phenotypic variance, especially  
465 for floral emergence known to be strongly affected by the environment (Jung et al., 2022).  
466 Although a large proportion of phenotypic variance was explained here by the enviromic-  
467 based effects, and these effects have been shown to positively influence predictive ability in  
468 other crops (Costa-Neto, Fritsche-Neto, et al., 2021; Jarquín et al., 2014), they have not  
469 resulted in any increase in predictive ability for apple traits. For productivity traits such as  
470 flowering intensity, which depends on flower bud formation during the previous vegetation  
471 season, the models could likely benefit from including prior-year environmental data in the  
472 construction of the enviromic matrix.

#### 473 **Alternative kernels**

474 Similar to previous reports that have shown increased predictive ability when Gaussian kernel  
475 and Deep kernel were applied (Costa-Neto, Fritsche-Neto, et al., 2021; Cuevas et al., 2019),  
476 these kernels resulted in a modest but significant improvement in predictive ability of 0.01–  
477 0.02 for most of the studied traits. The Gaussian kernel proved particularly suitable for  
478 capturing variance attributed to  $G \times E$ . Model structures based on the Deep kernel generally  
479 explained a smaller proportion of phenotypic variance than those using the Gaussian kernel  
480 and G-BLUP. This characteristic rendered Deep kernel less suitable for evaluating trait  
481 genetic architecture. Nevertheless, the Deep kernel-based models demonstrated improved  
482 predictive abilities, equivalent to those of Gaussian kernel-based models. Overall, both  
483 alternative kernels proved to be efficient substitutes for G-BLUP.

#### 484 **Deep learning for genomic prediction**

485 Specifically for each trait and cross-validation fold, the dimensional reduction of the marker  
486 dataset to a subset of 1,000 SNPs selected by a gradient boosting algorithm, extended with  
487 known marker-trait associations, allowed an efficient implementation of a deep learning  
488 approach for multi-environmental genomic prediction in apple. The studied deep learning  
489 approach combined feature streams derived from marker information with streams  
490 incorporating weather and soil variables. It resulted in stream contributions that effectively



491 represented trait genetic architectures described in this and previous studies using statistical  
492 genomic prediction models (Jung et al., 2022).

493 Our study demonstrated that the applied deep learning approach was particularly well-suited  
494 for oligogenic traits. For these traits, governed by a few genes, the dimensionality reduction of  
495 the marker dataset allowed important genomic information to be effectively represented. The  
496 trait genetic architecture for harvest date was particularly well captured, with a 72%  
497 contribution from the SNP stream. Harvest date was previously described as oligogenic trait  
498 with significant large-effect marker associations found on chromosomes 3, 10 and 16 using  
499 the apple REFPOP dataset (Jung et al., 2020, 2022). The strongest of these associations on  
500 chromosome 3 at 30.7 Mb (Jung et al., 2022) was located in a major locus *NAC18.1*  
501 associated with harvest date and multiple ripening traits (Migicovsky et al., 2016; Watts et al.,  
502 2023). The deep learning genomic prediction model proved efficient in capturing this major  
503 locus, as the three SNPs with the highest absolute mean SHAP were located on chromosome 3  
504 at 29.2, 30.7, and 30.8 Mb, the marker AX-115366114 at 30.7 Mb being strongly associated  
505 with harvest date according to our previous study (Jung et al., 2022). Moreover, the deep  
506 learning genomic prediction model outperformed the benchmark statistical genomic  
507 prediction model G for harvest date, improving predictive ability by 0.06 and achieving the  
508 highest predictive ability among all tested models at 0.75.

509 Red over color has shown similar predictive ability and trait genetic architecture as harvest  
510 date in this and previous studies based on statistical genomic prediction models (Jung et al.,  
511 2022). The SNPs associated with *MdMYB1* transcription factor on chromosome 9, which  
512 regulates red pigmentation of apple skin (Tacos et al., 2006), translated into large absolute  
513 mean SHAP values and predictive ability improved by 0.10 compared to model G. Similar  
514 results were observed for titratable acidity, where large absolute mean SHAP were found, and  
515 the three SNPs with the largest SHAP were located on chromosome 8 at 10.7, 10.8, and 11.8  
516 Mb. Two large-effect loci are known for acidity in apple, namely *Ma* on chromosome 16 and  
517 *Ma3* on chromosome 8 (Verma et al., 2019). The SNPs on chromosome 8 indicated a strong  
518 association with the *Ma3* locus, and they colocalized with the SNP marker predictive for this  
519 locus at 10.9 Mb (Rymenants et al., 2020). The maximum relative SHAP contribution for the  
520 SNP stream of 80% was reached for titratable acidity. Moreover, the predictive ability of the  
521 deep learning genomic prediction model for titratable acidity was improved by 0.07 compared  
522 to the statistical genomic prediction model G. Our results for harvest date, red over color, and  
523 titratable acidity showed that high relative and absolute SHAP values can serve as predictors  
524 of improved deep learning genomic prediction model performance, and that the applied deep  
525 learning approach can precisely predict apple traits characterized by oligogenic architecture.

526 According to Montesinos-López et al. (2021), the predictive ability of deep learning  
527 approaches typically falls below that of conventional models for genomic prediction, unless  
528 very large datasets are examined. In our study, the sizes of datasets showed large differences  
529 between the three traits with predictive ability superior to all other compared statistical  
530 genomic prediction models (total number of training instances of 12,428 for harvest date,  
531 10,317 for red over color, and 2,879 for titratable acidity, Table S1). Although the number of  
532 available environments ranged from the minimum of eight for titratable acidity to the  
533 maximum of 25 for harvest date, similar improvement in predictive ability was reached for

534 these traits using the applied deep learning approach. As the improvements in predictive  
535 ability for harvest date, red over color, and titratable acidity were observed independently  
536 from the number of training instances, the size of the phenotypic dataset is unlikely to have  
537 affected our predictions. Nevertheless, an additional improvement in predictive ability for the  
538 deep learning model may be anticipated by increasing the training population size in terms of  
539 the number of genotypes.

#### 540 **Multi-environmental genomic selection in apple breeding**

541 The establishment of multi-environmental genomic selection in apple has been constrained by  
542 several factors, including the costly collection of extensive multi-environmental datasets and  
543 computational limitations. The phenotyping efforts in the apple REFPOP yielded an  
544 unprecedented dataset in terms of trait-environment combinations (Jung et al., 2022), which  
545 has been expanded in this study with two additional years of phenotyping. This dataset now  
546 encompasses phenotypic data for eleven traits across up to 25 environments. The availability  
547 of this dataset has enabled the implementation of multi-environmental genomic prediction  
548 models within a computationally efficient framework, laying the groundwork for the practical  
549 application of multi-environmental genomic selection in apple. Further insights into predictive  
550 ability for independent test sets could be gained in the future by assessing the predictive  
551 performance on breeding material distinct from the apple REFPOP. Additionally, expanding  
552 the training set size may increase predictive ability for some traits (Minamikawa et al., 2024)  
553 and could potentially enable a more accurate estimation of variance components. To expand  
554 the dataset by increasing the number of genotypes and environments, new collaborative  
555 approaches between breeders are required to generate data capable of overcoming this  
556 challenge.

557 The approach to multi-environmental genomic prediction of apple traits used in this study  
558 diverges from the traditional understanding of environments in apple tree cultivation. In  
559 practice, apple trees remain stationary in the same location across multiple years. This  
560 stationary nature of apple cultivation implies that the effects of yearly climatic variations are  
561 superimposed on the same geographical location, whereas the genomic prediction approach  
562 treats each year-location combination as a distinct environment. Nevertheless, breeding values  
563 for apple genotypes lacking phenotypic information can be predicted across diverse  
564 environmental conditions using the genomic prediction models trained in this study.

565 Among all predictions obtained, the model  $G+G \times E$  applying Gaussian and Deep kernels  
566 improved predictive abilities for most traits (except for titratable acidity and fruit firmness,  
567 where it showed results comparable to those of the benchmark model  $G$ ). Therefore, the  
568 model  $G+G \times E$  proved to be a universally effective solution for multi-environmental genomic  
569 prediction in the studied apple traits. Additionally, the  $G+G \times E$  model, along with other  
570 statistical genomic prediction models tested, was outperformed by the applied deep learning  
571 approach for three traits with oligogenic genetic architectures (harvest date, titratable acidity,  
572 and red over color). Depending on the genetic architecture of the trait, either the  $G+G \times E$   
573 model or the deep learning approach can be recommended for multi-environmental genomic  
574 predictions, leading to informed breeding decisions, and assisting in the selection of cultivars  
575 more adaptable to future climates.

## 576 MATERIALS AND METHODS

### 577 Plant material

578 The apple REFPOP comprised 265 progenies from 27 biparental families generated by  
579 European breeding programs, along with 269 diverse accessions (Jung et al., 2020). This  
580 study focused on five locations: (i) Rillaar, Belgium, (ii) Angers, France, (iii) Laimburg, Italy,  
581 (iv) Lleida, Spain, and (v) Waedenswil, Switzerland. At each location, all genotypes were  
582 generally represented by two trees and planted in 2016 using a randomized complete block  
583 design. Three control genotypes, namely 'Gala', 'Golden Delicious', and 'CIVG198', were  
584 replicated up to 22 times at each location. The cultivation followed the common agricultural  
585 practices specific to each location, incorporating integrated plant protection methods.

### 586 Phenotyping

587 Phenotyping of the eleven traits followed the methodology described by Jung et al. (2022).  
588 Individual trees, representing genotype replicates, were used for trait measurement. Floral  
589 emergence was determined in Julian days, marking the date when the first 10% of flowers  
590 opened. Flowering intensity was evaluated on a nine-grade scale, indicating the percentage of  
591 existing flowers relative to the maximum potential number of flowers. Fruits were harvested  
592 on harvest dates, determined in Julian days, based on expert estimates of fruit ripening. Total  
593 fruit weight (kg) and fruit number were recorded to assess production per tree. Single fruit  
594 weight (g) was estimated by dividing the total fruit weight by the number of fruits. Titratable  
595 acidity (g/l), soluble solids content ( $^{\circ}$ Brix), and fruit firmness ( $\text{g}/\text{cm}^2$ ) were measured within  
596 one week post-harvest using an automated instrument Pimprenelle (Setop, France). Red over  
597 color, representing the percentage of red fruit skin, was assessed on a six-grade scale. Russet  
598 frequency indicated the percentage of fruits exhibiting russet skin. Further information  
599 regarding the evaluation of the eleven traits is available in Jung et al. (2022). For the different  
600 traits, the assessment spanned a period of up to five years from 2018 to 2022 and was  
601 performed at up to five locations.

### 602 Envirotyping

603 Hourly measurements of temperature ( $^{\circ}\text{C}$ ) at 2 m above soil level, relative humidity (%) and  
604 global radiation ( $\text{W}/\text{m}^2$ ) were obtained from the weather stations near the apple REFPOP  
605 orchards from 2018 to 2022. Precipitation (mm) was not taken into consideration in this study  
606 due to irrigation practices in part of the orchard locations.

607 In each apple REFPOP orchard between May 12 and June 9, 2016, a total of six soil samples  
608 were collected from three distinct sampling points and two soil depths (approximately 1–20  
609 cm and 20–40 cm). In the accredited Laboratory for Soil and Plant Analysis of Laimburg  
610 Research Centre, Italy, the soil samples were analyzed for (i) organic carbon (% humus), (ii)  
611 pH, (iii) carbonate test, expressed as low to medium, high, very high or no carbonate content,  
612 (iv) carbonate requirement ( $\text{dt}/\text{ha}$  CaO), (v) phosphorus ( $\text{mg}/100$  g  $\text{P}_2\text{O}_5$ ), (vi) potassium  
613 ( $\text{mg}/100$  g  $\text{K}_2\text{O}$ ), (vii) magnesium ( $\text{mg}/100$  g), (viii) boron ( $\text{mg}/\text{kg}$ ), (ix) manganese ( $\text{mg}/\text{kg}$ ),  
614 (x) copper ( $\text{mg}/\text{kg}$ ), and (xi) zinc ( $\text{mg}/\text{kg}$ ).

### 615 Genotyping

616 As detailed by Jung et al. (2020), the apple REFPOP underwent genotyping for biallelic single  
 617 nucleotide polymorphisms (SNPs) through a dual approach utilizing the Illumina Infinium®  
 618 20K SNP genotyping array (Bianco et al., 2014) and the Affymetrix Axiom® Apple 480K  
 619 SNP genotyping array (Bianco et al., 2016). By employing the Beagle 4.0 software (Browning  
 620 & Browning, 2007) and incorporating pedigree information (Muranty et al., 2020), the  
 621 obtained SNP sets were integrated through imputation, ultimately yielding a genomic dataset  
 622 of 303,239 biallelic SNPs. All SNP positions were based on the doubled haploid GDDH13  
 623 (v1.1) reference genome (Daccord et al., 2017).

## 624 Phenotypic data preprocessing

625 Analyses of phenotypic data were conducted to ensure high data quality by addressing low  
 626 heritability, spatial heterogeneity, and eliminating outliers. The statistical model for the  
 627 phenotypic data preprocessing was fitted via restricted maximum likelihood using the R  
 628 package ‘lme4’ (v.1.1-28) (Bates et al., 2015) as:

$$629 \quad \mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{Z}\mathbf{u} + \boldsymbol{\varepsilon} \quad (\text{Equation 1})$$

630 where  $\mathbf{y}$  was the vector of the response variable,  $\mathbf{X}$  the design matrix for the fixed effects,  $\boldsymbol{\beta}$   
 631 the vector of the fixed effects,  $\mathbf{Z}$  was the design matrix for the random effects,  $\mathbf{u}$  the vector of  
 632 the random effects assuming  $\mathbf{u} \sim N(0, \boldsymbol{\Sigma})$  with  $\boldsymbol{\Sigma}$  being the variance–covariance matrix of the  
 633 random effects and  $\boldsymbol{\varepsilon}$  the vector of the random errors assuming  $\boldsymbol{\varepsilon} \sim N(0, \sigma_{\varepsilon}^2 \mathbf{I})$  with  $\sigma_{\varepsilon}^2$  being  
 634 the error variance and  $\mathbf{I}$  the identity matrix.

635 Separately for each trait and environment (combined factor of location and year), raw  
 636 phenotypic values for each genotype replicate (total fruit weight and fruit number were log-  
 637 transformed) were used as response variable to fit a random-effects model with a random  
 638 effect of genotype following the Equation 1. From the variance components of the random-  
 639 effects model, the environment-specific clonal mean heritability was calculated as:

$$H^2 = \frac{\sigma_g^2}{\sigma_g^2 + \frac{\sigma_{\varepsilon}^2}{\bar{n}_t}}$$

640 where  $\sigma_g^2$  was the genotypic variance and  $\bar{n}_t$  the mean number of genotype replications. The  
 641 environment-specific clonal mean heritability was used to remove trait-environment  
 642 combinations with the heritability value below 0.1.

643 To account for spatial variation in the orchards, spatial heterogeneity in the raw phenotypic  
 644 data was modeled separately for each trait-environment combination using the spatial analysis  
 645 of field trials with splines (‘SpATS’ (v.1.0-11)) (Rodríguez-Álvarez et al., 2018) as described  
 646 by Jung et al. (2020). From the fitted SpATS objects, the adjusted phenotypic values of each  
 647 genotype and the adjusted phenotypic values of each tree were obtained.

648 The adjusted phenotypic values of each genotype were used as response variable for fitting a  
 649 mixed-effects model with a fixed effect of environment and a random effect of genotype  
 650 following Equation 1. Subsequently, the outliers were detected using Bonferroni–Holm test to  
 651 judge residuals standardized by the re-scaled median absolute deviation (BH-MADR) as  
 652 described by Bernal-Vasquez et al. (2016). The identified outliers were removed and the



653 remaining trait- and environment-specific adjusted phenotypic values of each genotype were  
 654 further denoted as adjusted means. The adjusted means for the eleven studied traits were  
 655 compared separately for each year and location using the pairwise Pearson's correlations and  
 656 significance tests implemented in the R package 'corrplot' (v.0.92) (Wei & Simko, 2021). The  
 657 significance levels of 0.05, 0.01, and 0.001 were Bonferroni-corrected by dividing them by  
 658 the total number of pairwise comparisons among the eleven traits.

659 Following Equation 1, the adjusted phenotypic values of each tree served as the response  
 660 variable in fitting a mixed-effects model, denoted here as the phenotypic model. This model  
 661 included the fixed effects of environment (E), the random effects of genotype (g), and random  
 662 effects of genotype-by-environment interaction ( $g \times E$ ). The proportions of phenotypic variance  
 663 explained by the random effects were extracted from the model fit for comparison with the  
 664 statistical genomic prediction models.

### 665 **Enviromic data preprocessing**

666 The enviromic data were restructured to acquire appropriate inputs for the subsequent  
 667 modelling. Daily temperature means, daily humidity means, and daily radiation sums were  
 668 calculated from the hourly measurements. These three daily weather variables were visualized  
 669 applying local regression curves estimated using Loess with a span of 0.1.

670 Inspired by Jarquín et al. (2014), the three daily weather variables were processed to create six  
 671 environmental covariates by dividing each growing season into two periods based on crop  
 672 phenology. The two periods were defined separately for each environment. The first period  
 673 extended for 80 days, concluding on the day when 90% of the genotypes flowered,  
 674 determined from adjusted means for floral emergence. The second period followed the first  
 675 until the day when 90% of the genotypes were harvested, as indicated by the adjusted means  
 676 for harvest date. Different approaches to defining the first period were employed for two  
 677 environments where adjusted means for floral emergence were unavailable. In the case of the  
 678 environment ESP.2020, which was excluded due to low heritability, the adjusted phenotypic  
 679 values of each genotype were used to estimate the day when 90% of the genotypes flowered.  
 680 For ESP.2022, where floral emergence scores were missing, the end date of the first period  
 681 was estimated based on varieties cultivated near the apple REFPOP. Daily temperature means,  
 682 daily humidity means, and daily radiation sums were summed over each respective period,  
 683 resulting in six environmental covariates. Additionally, 22 environmental covariates were  
 684 obtained as mean values of eleven soil characteristics calculated per location and the level of  
 685 soil depth. All 28 environmental covariates were collected in the  $q \times z$  matrix of  
 686 environmental covariates  $M_W$  with  $q$  environments and  $z$  environmental covariates, which  
 687 was then scaled and centered to the mean of zero and standard deviation of one.

### 688 **Marker matrices**

689 Three marker matrices were constructed based on the genomic dataset of biallelic SNPs. The  
 690 first matrix followed the standard allele coding, where a SNP was assigned the value 0 when  
 691 the individual (i.e., genotype) was homozygous for the first allele ( $a$ ), 1 when the genotype  
 692 was heterozygous, and 2 when the genotype was homozygous for the second allele ( $A$ ). The  
 693 allele coding can be referred to as coefficients in the marker matrix. Therefore, the  $n \times m$

694 marker matrix of the standard coefficients  $\mathbf{M}_G$  with  $i = 1, \dots, n$  genotypes and  $j = 1, \dots, m$   
 695 markers was:

$$\mathbf{M}_G = \begin{bmatrix} h_{G_{11}} & \cdots & h_{G_{1m}} \\ \vdots & \ddots & \vdots \\ h_{G_{n1}} & \cdots & h_{G_{nm}} \end{bmatrix}$$

696 where the element  $h_{G_{ij}}$  for the  $i$ th genotype and  $j$ th marker was equal to:

$$697 \quad h_{G_{ij}} = \begin{cases} 2 & \text{for } \begin{cases} AA \\ Aa \\ aa \end{cases} \\ 1 & \\ 0 & \end{cases}$$

698 with  $AA$ ,  $Aa$  and  $aa$  being the combinations of the alleles  $a$  and  $A$  at the marker  $j$ . Each  
 699 column of the matrix  $\mathbf{M}_G$  was scaled and centered to the mean of zero and standard deviation  
 700 of one.

701 The second and third marker matrices followed the NOIA model (Álvarez-Castro & Carlborg,  
 702 2007) as implemented by Vitezica et al. (2017). These matrices were estimated from the  
 703 elements of the marker matrix of the standard coefficients  $\mathbf{M}_G$  and had the same dimension.  
 704 The element  $h_{A_{ij}}$  for the  $n \times m$  marker matrix of additive coefficients  $\mathbf{M}_A$  and the element  
 705  $h_{D_{ij}}$  for the  $n \times m$  marker matrix of dominance coefficients  $\mathbf{M}_D$  were calculated as follows:

$$706 \quad h_{A_{ij}} = \begin{cases} -(-p_{Aa} - 2p_{aa}) & \text{for } \begin{cases} AA \\ Aa \\ aa \end{cases} \\ -(1 - p_{Aa} - 2p_{aa}) & \\ -(2 - p_{Aa} - 2p_{aa}) & \end{cases}$$

707 and

$$708 \quad h_{D_{ij}} = \begin{cases} -\frac{2p_{Aa}p_{aa}}{p_{AA}+p_{aa}-(p_{AA}-p_{aa})^2} & \text{for } \begin{cases} AA \\ Aa \\ aa \end{cases} \\ \frac{4p_{AA}p_{aa}}{p_{AA}+p_{aa}-(p_{AA}-p_{aa})^2} & \\ -\frac{2p_{AA}p_{Aa}}{p_{AA}+p_{aa}-(p_{AA}-p_{aa})^2} & \end{cases}$$

709 with  $p_{AA}$ ,  $p_{Aa}$  and  $p_{aa}$  being the relative frequencies for the allelic combinations  $AA$ ,  $Aa$  and  
 710  $aa$  at marker  $j$ .

### 711 Relationship matrices

712 The marker matrices  $\mathbf{M}_G$ ,  $\mathbf{M}_A$  and  $\mathbf{M}_D$  and the matrix of environmental covariates  $\mathbf{M}_W$  were  
 713 used to estimate the standard genomic relationship matrix  $\mathbf{K}_G$ , the additive genomic  
 714 relationship matrix  $\mathbf{K}_A$ , the dominance genomic relationship matrix  $\mathbf{K}_D$ , and the enviromic  
 715 relationship matrix  $\mathbf{K}_W$ , respectively. Initially, all relationship matrices were created based on  
 716 the genomic best linear unbiased predictor (G-BLUP) approach described by VanRaden  
 717 (2008). The covariance matrix following the G-BLUP approach was obtained as:

$$\mathbf{K} = \frac{\mathbf{M}\mathbf{M}'}{\text{tr}(\mathbf{M}\mathbf{M}')/\text{nrow}(\mathbf{M})}$$

718 where  $\mathbf{K}$  was a generic representation of the relationship matrix ( $\mathbf{K}_G$ ,  $\mathbf{K}_A$ ,  $\mathbf{K}_D$  and  $\mathbf{K}_W$ ),  $\mathbf{M}$   
 719 was a generic representation of the marker matrices  $\mathbf{M}_G$ ,  $\mathbf{M}_A$  and  $\mathbf{M}_D$  as well as the matrix of  
 720 environmental covariates  $\mathbf{M}_W$ , and  $nrow$  was the number of genotypes for  $\mathbf{M}_G$ ,  $\mathbf{M}_A$  and  $\mathbf{M}_D$   
 721 or the number of environments for  $\mathbf{M}_W$ .

722 Subsequently, two covariance matrix types, namely the Gaussian kernel (González-Camacho  
 723 et al., 2012) and Deep kernel (Cuevas et al., 2019), were examined as alternatives to the G-  
 724 BLUP approach. The Gaussian kernel is a nonlinear method based on a bandwidth parameter  
 725 that controls the decay rate of covariance between genotypes, and the percentile of the square  
 726 of the Euclidean distance, which is a metric reflecting the genetic distance between genotypes.  
 727 The Deep kernel is characterized by a nonlinear arc-cosine function, and its covariance matrix  
 728 is designed to mimic a deep-learning model featuring a single hidden layer with many  
 729 neurons. Applying these alternative approaches, the standard genomic and enviromic  
 730 relationship matrices based on Gaussian kernel ( $\mathbf{K}_{G_{GK}}$  and  $\mathbf{K}_{W_{GK}}$ ) and Deep kernel ( $\mathbf{K}_{G_{DK}}$  and  
 731  $\mathbf{K}_{W_{DK}}$ ) were created. The Gaussian kernel and Deep kernel were implemented following the  
 732 estimation process as detailed by Costa-Neto, Fritsche-Neto, et al. (2021).

### 733 Statistical genomic prediction model structures

734 The relationship matrices were used to create linear mixed model structures for the statistical  
 735 genomic prediction models. Following Costa-Neto, Fritsche-Neto, et al. (2021), the generic  
 736 model structure was defined as:

$$737 \quad \mathbf{y} = \mathbf{1}\boldsymbol{\mu} + \mathbf{X}_f\boldsymbol{\beta} + \sum_{s=1}^k \mathbf{g}_s + \sum_{r=1}^l \mathbf{w}_r + \boldsymbol{\varepsilon} \quad (\text{Equation 2})$$

738 where  $\mathbf{y}$  was the vector of the adjusted means for  $n$  genotypes across  $q$  environments,  $\mathbf{1}\boldsymbol{\mu}$  was  
 739 the overall mean,  $\mathbf{X}_f$  the design matrix for the fixed effects of environments,  $\boldsymbol{\beta}$  the vector of  
 740 the fixed effects,  $\mathbf{g}_s$  the random vector for  $s = 1, \dots, k$  marker-based effects,  $\mathbf{w}_r$  the random  
 741 vector for  $r = 1, \dots, l$  enviromic-based effects, and  $\boldsymbol{\varepsilon}$  the vector of the random errors assuming  
 742  $\boldsymbol{\varepsilon} \sim N(0, \sigma_\varepsilon^2 \mathbf{I})$  with  $\sigma_\varepsilon^2$  being the error variance and  $\mathbf{I}$  the identity matrix. The effects of  
 743 environments were modeled as fixed in all model structures tested, consistent with other  
 744 multi-environmental models that incorporate G×E, as described by, e.g., Lopez-Cruz et al.  
 745 (2015) and Costa-Neto, Fritsche-Neto, et al. (2021). All model structures were based on the  
 746 G-BLUP approach to estimating the relationship matrices. When the alternatives to the G-  
 747 BLUP were used, the model structures were additionally labeled with '(GK)' for the Gaussian  
 748 kernel and '(DK)' for the Deep kernel. For all three approaches to estimating the relationship  
 749 matrices, the function `get_kernel` of the R package 'EnvRtype' (v.1.1.1) (Costa-Neto, Galli, et  
 750 al., 2021) was used to obtain the relationship matrices for genomic prediction.

751 **Models G, A, and G+D (random (main) genotypic effects (MM)).** Following the Equation  
 752 2, the model MM accounted for the marker-based effects ( $\sum_{s=1}^k \mathbf{g}_s \neq 0$ ) without applying the  
 753 enviromic-based effects ( $\sum_{r=1}^l \mathbf{w}_r = 0$ ). The  $\mathbf{g}_s$  incorporated relationship matrices  $\mathbf{K}_G$   
 754 (alternatively  $\mathbf{K}_{G_{GK}}$  or  $\mathbf{K}_{G_{DK}}$ ),  $\mathbf{K}_A$  and  $\mathbf{K}_D$  representing random genomic (G), additive (A) and  
 755 dominance (D) effects, respectively. These effects were applied individually or in  
 756 combinations, resulting in model structures denoted as G (alternatively G (GK) and G (DK)),  
 757 A and G+D.

758 **Models G+G×E and G+G×E+D+D×E (single variance genotype × environment deviation**  
 759 **(MDs)).** Analogous to the model MM, the model MDs assumed  $\sum_{s=1}^k \mathbf{g}_s \neq 0$  and  $\sum_{r=1}^l \mathbf{w}_r =$   
 760 0 (Equation 2). In addition to the random effects G and D, the random interaction effects (×)  
 761 with the vector of environments (E) were included, namely the G×E and D×E. This resulted in  
 762 model structures G+G×E (alternatively G+G×E (GK) and G+G×E (DK)) and  
 763 G+G×E+D+D×E.

764 **Model G+W (enviromic-enriched MM (EMM)).** The model EMM applied both the marker-  
 765 based effects ( $\sum_{s=1}^k \mathbf{g}_s \neq 0$ ) and the enviromic-based effects ( $\sum_{r=1}^l \mathbf{w}_r \neq 0$ ) (Equation 2).  
 766 Included were the random effects G and the random enviromic effects (W), the latter being  
 767 derived through the integration of the relationship matrix  $\mathbf{K}_W$  (alternatively  $\mathbf{K}_{W_{GK}}$  and  $\mathbf{K}_{W_{DK}}$ ).  
 768 The resulting model structure was G+W (alternatively G+W (GK) and G+W (DK)).

769 **Model G+W+G×W (reaction-norm MM (RNMM)).** Building upon the model EMM, the  
 770 model RNMM ( $\sum_{s=1}^k \mathbf{g}_s \neq 0$  and  $\sum_{r=1}^l \mathbf{w}_r \neq 0$ , Equation 2) extended the random enviromic-  
 771 based effects with a random interaction effect G×W. The obtained model structure was  
 772 G+W+G×W (alternatively G+W+G×W (GK) and G+W+G×W (DK)).

773 **Model G+G×E+W+G×W (reaction-norm MDs (RNMDs)).** The last of the compared  
 774 models, the model RNMDs ( $\sum_{s=1}^k \mathbf{g}_s \neq 0$  and  $\sum_{r=1}^l \mathbf{w}_r \neq 0$ , Equation 2), combined the  
 775 random marker-based effects G and G×E with the random enviromic-based effects W and  
 776 G×W in a single model structure G+G×E+W+G×W (alternatively G+G×E+W+G×W (GK)  
 777 and G+G×E+W+G×W (DK)).

778 **Fixed effect of inbreeding.** The design matrix for the fixed effects  $\mathbf{X}_f$  (Equation 2) was based  
 779 on the vector of environments (E) for all model structures tested in this study. As described by  
 780 previous authors (Roth et al., 2022; Vitezica et al., 2018), including an inbreeding coefficient  
 781 as fixed effect can account for directional dominance effects and help to avoid overestimating  
 782 the proportion of variance explained by the dominance model components. Hence, the model  
 783 MM was additionally extended with the fixed effect of inbreeding contained in parameter  $\mathbf{X}_f$ ,  
 784 which was incorporated in the model structures denoted as G (inb) and G+D (inb). The  
 785 inbreeding coefficient for each genotype was estimated from the marker matrix  $\mathbf{M}_G$ ,  
 786 calculated as the relative frequency of the homozygous allelic combinations AA and aa across  
 787 all markers.

## 788 **Deep learning approach**

789 The deep learning genomic prediction model was designed to be able to receive both  
 790 genotypic and environmental data in the form of four streams. Genotypic data underwent  
 791 feature selection in two different ways, generating input data for two different streams of the  
 792 model: single nucleotide polymorphism (SNP) stream and principal component (PC) stream.  
 793 First, to represent specific genetic variation, the most relevant 1,000 SNPs for each trait and  
 794 fold were extracted from the marker matrix  $\mathbf{M}_G$  with a gradient boosting regressor. The  
 795 response variable for the gradient boosting model was derived from the means of the random  
 796 effects of genotypes, which were extracted from a mixed-effects model. This mixed-effects  
 797 model followed Equation 1, incorporating fixed effects of the environment (E) and random



798 effects of genotype (g). Additionally, the SNPs associated with the studied traits as reported  
799 by Jung et al. (2022) were added to the existing pool of 1,000 SNPs within the SNP stream.  
800 Second, using the principal component analysis in related samples (PC-AiR) method (Kick et  
801 al., 2023), 58 principal components (PCs) capturing 100% of the genetic variation were  
802 extracted and used as input to represent the overall genetic variation. Daily weather variables  
803 and soil environmental covariates directly constituted the input for the weather and soil  
804 streams, respectively. The adjusted phenotypic means served as the response variables. All  
805 stream and response variables were scaled between -1 and 1. The model architecture was  
806 designed using 'TensorFlow' (v.2.10.0) and 'Keras' (v.2.10.0). All streams consisted of a  
807 variable number of dense layers except for the weather stream. In this case, the first layers  
808 were long short-term memory (LSTM), which excel at processing sequential data. The four  
809 streams processed the data independently and were concatenated after several layers. Further  
810 dense layers were placed before the output neuron to allow for data integration. For specific  
811 details on the model architecture, please refer to the provided GitHub link  
812 (<https://github.com/MichaelaJung/Integrative-prediction>). Models for each trait were trained  
813 and evaluated at different learning rates ( $1e^{-4}$ ,  $1e^{-5}$ , and  $5e^{-6}$ ). When the training loss stopped  
814 improving, the training was stopped. The appropriate learning rate was decided for each trait  
815 based on the highest correlation and the lowest root mean squared error.

## 816 **Genomic prediction**

817 All statistical and deep learning genomic prediction models were iteratively fitted in a five-  
818 fold cross-validation that was repeated five times, with genotypes being allocated to folds  
819 randomly and without replacement, resulting in 25 runs of each tested model. All models  
820 were applied using the same genotype allocations for each fold. The statistical genomic  
821 prediction model structures were solved using Bayesian hierarchical modeling implemented  
822 in the R package 'BGGE' (v.0.6.5) (Granato et al., 2018). The statistical genomic prediction  
823 models underwent 10,000 iterations of the Gibbs sampler, employing a thinning of 3 and  
824 discarding the initial 1,000 samples as burn-in.

## 825 **Relative contribution of model components**

826 For the statistical genomic prediction models, each model fit from the cross-validation was  
827 used to obtain the proportions of variance explained by the various random effects. To explain  
828 the deep learning model predictions with respect to each input feature (e.g., a SNP or weather  
829 variable), the 'GradientExplainer' function from the 'shap' package (v.0.42.1) (Lundberg &  
830 Lee, 2017) was used to calculate approximated Shapley additive explanations (SHAP). It uses  
831 the gradients of the model to approximate SHAP values for each feature, which estimates  
832 their contribution to the prediction. SHAP values were calculated for every instance of every  
833 test fold in each repetition of the cross-validation. The absolute values of each feature were  
834 averaged to obtain absolute mean SHAP values per feature. Furthermore, to investigate the  
835 contribution of each stream to the prediction, the absolute mean SHAP values were summed  
836 for every fold, and the relative SHAP contribution of each stream was obtained as a  
837 percentage.

## 838 **Assessment of predictive ability**

839 For every statistical and deep learning genomic prediction model and trait, twenty-five  
840 estimates of predictive ability were generated for each environment, calculated as Pearson's  
841 correlation coefficient between the adjusted means and predicted values. This resulted in 200  
842 predictive ability estimates for titratable acidity, soluble solids content, and fruit firmness, 500  
843 for russet frequency, 525 for red over color, 575 for floral emergence and flowering intensity,  
844 and 625 for harvest date, total fruit weight, number of fruits, and single fruit weight. Average  
845 predictive ability across traits was calculated by averaging all estimates of predictive ability  
846 for each model.

847 Four models were selected for an in-depth comparison based on their performance and  
848 characteristics. The selection criteria included improvements of at least 0.01 in average  
849 predictive ability across traits compared to the benchmark model G. Additionally, statistical  
850 genomic prediction models that explained a large proportion of variance were prioritized, with  
851 a preference for simpler model structures over more complex ones. For each of these models,  
852 both the average predictive ability and the distribution of predictive abilities were visualized  
853 and compared with those of the model G for every trait.

854 All statistical analyses in this work were implemented in R (v.4.1.3) (R Core Team, 2022).  
855 The code for implementing, training, using, and explaining the deep learning genomic  
856 prediction models was written in Python (v.3.9.16).

857

## 858 **ACKNOWLEDGMENTS**

859 The authors thank the field technicians and staff at INRAe IRHS and Experimental Unit (UE  
860 Horti), Angers, France, the Fruit Breeding Group at Agroscope in Wädenswil, Switzerland,  
861 and technical staff at all apple REFPOP sites for the maintenance of the orchards and  
862 phenotypic data collection. Phenotypic data collection was partially supported by the Horizon  
863 2020 Framework Program of the European Union under grant agreement No 817970 (project  
864 INVITE: "Innovations in plant variety testing in Europe to foster the introduction of new  
865 varieties better adapted to varying biotic and abiotic conditions and to more sustainable crop  
866 management practices"). C.Q.-T. was supported by the European Union's Horizon 2020  
867 research and innovation program under the Marie Skłodowska-Curie grant agreement No  
868 847585 – RESPONSE. This study was partially funded by the FOAG project "Apfelzukunft  
869 dank Züchtung" (2020/17/AZZ).

870

## 871 **AUTHOR CONTRIBUTIONS**

872 This research was conceived by M.J., M.Roth, M.J.A., W.G., F.L., H.M., B.S., and A.P. M.J.,  
873 M.R., E.H., N.P., L.L., and F.D. contributed to data collection. M.J. carried out the statistical  
874 data analysis with the support of M.Roth., G.B., and A.P. C.Q.-T. performed the deep learning  
875 analysis in consultation with M.J., S.Y., and B.S. M.J. and C.Q.-T. wrote the article in  
876 consultation with M.Roth, M.J.A., H.M., M.R., W.G., F.L., S.Y., B.S., G.B., and A.P. All  
877 authors have read the manuscript and approved the version to be published.

878

879 **DATA AVAILABILITY**

880 All SNP genotypic data used in this study have been deposited in the INRAe dataset archive  
881 at <https://doi.org/10.15454/IOPGYF> and <https://doi.org/10.15454/1ERHGX>. The raw  
882 phenotypic data are available in the INRAe dataset archive at  
883 <https://doi.org/10.15454/VARJYJ>. The code underlying this article is available in GitHub at  
884 <https://github.com/MichaelaJung/Integrative-prediction>. The phenotypic, enviromic, and  
885 imputed genomic data formatted as input files for the provided code are available in Zenodo  
886 at [to be updated upon article release].

887

888 **CONFLICT OF INTERESTS**

889 The authors declare no conflicts of interest.

890

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